2021 IUT Admission Test(SBL)

Math Examination

Essay Types> Applicants should write detailed solving process. If there is no solution, you will receive 0 points regardless of the correct answer.

- O The point for each question is indicated next to each question number.
- 4. [5 points] Find $\cos \frac{\pi}{8}$.

1. [5 points]

When
$$\alpha^2 = \sqrt{3+2\sqrt{2}}$$
, find $\frac{\alpha^3 - \alpha^{-3}}{\alpha - \alpha^{-1}}$.



2. [5 points]

Evaluate
$$\log_3 \frac{243}{2} - \log_9 \frac{81}{4}$$
.

5. [10 points]

When
$$\begin{pmatrix} 1 & 2 \\ 0 & 1 \end{pmatrix}^{100} = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$$
, find $a+b+c+d$.



3. [5 points]

When
$$a = \frac{\sqrt{3} + i}{2}$$
, find a^{100} .

6. [10 points]

When an arithmetic sequence $\{a_n\}_{n=1}^{\infty}$ satisfies $a_1+a_3=12,\,a_7+a_9=34$, find a_{13} . Here an arithmetic sequence means a sequence $\{a_n\}_{n=1}^{\infty}$ such that a_n-a_{n-1} is constant for all n.

7. [10 points]

Find $\lim_{\theta \to 0} \frac{1 - \cos \theta}{\sin \theta \ tg \theta}$.

8. [10 points]

When
$$f(x) = \frac{(2x^2 - 3x + 2)^{50}}{x^2 + 1}$$
, find $f'(1)$.

9. [20 points]

Find
$$\lim_{n \to \infty} \frac{1^4 + 2^4 + 3^4 + \dots + n^4}{n^5}$$
.

10. [20 points]

Find the area of the region enclosed by $y = x^2 - 3x + 1$ and $y = -x^2 - x + 5$.