

IUT 1st Admission Test(SBL)  
**Math Examination(TYPE A)**

< Multiple choice Types > There is only one correct answer for each question. Mark your choice on the OMR answer sheet.

- The points for each question are listed next to the question number.
- You can use the right side of each page for your memo.

1. [3 points]

Find  $(1 + \sqrt{2})^4 + (1 - \sqrt{2})^4$ .

- ① 30    ② 32    ③ 34    ④ 36    ⑤ 38

2. [3 points]

When  $a + b + c = 1$ ,  $a^2 + b^2 + c^2 = 5$  and

$\frac{1}{a} + \frac{1}{b} + \frac{1}{c} = 3$ , find  $abc$ .

- ①  $\frac{2}{3}$     ②  $\frac{4}{3}$     ③ 0    ④  $-\frac{2}{3}$     ⑤  $-\frac{4}{3}$

3. [3 points]

When  $\alpha$  and  $\beta$  are the solutions of  $x^2 + 5x + 2 = 0$ , find  $\alpha^3 + \alpha\beta + \beta^3$ .

- ① -91    ② -93    ③ -95    ④ -97    ⑤ -99

4. [3 points]

When  $t - \frac{1}{t} = 2\sqrt{3}$  and  $t > 0$ , find  $t^3 + \frac{1}{t^3}$ .

- ① 50    ② 52    ③ 54    ④ 56    ⑤ 58

5. [3 points]

Find  $\sum_{n=1}^{10} \frac{1}{n^2 + 4n + 3}$ .

- ①  $\frac{31}{104}$     ②  $\frac{33}{104}$     ③  $\frac{35}{104}$     ④  $\frac{37}{104}$     ⑤  $\frac{39}{104}$

6. [3 points]

When  $(a_1, b_1)$  and  $(a_2, b_2)$  are solutions of

$$\begin{cases} x^2 + y^2 = 2 \\ 2x + y = 1, \end{cases}$$

find  $a_1 + b_1 + a_2 + b_2$ .

- ①  $-\frac{4}{5}$     ②  $-\frac{2}{5}$     ③ 0    ④  $\frac{3}{5}$     ⑤  $\frac{6}{5}$

7. [3 points]

Simplify

$\log_3(\sqrt{2} + \sqrt{8} + \sqrt{9}) + \log_3(\sqrt{2} + \sqrt{8} - \sqrt{9})$ .

- ① 2    ② 3    ③  $\sqrt{2}$     ④  $\sqrt{3}$     ⑤  $\sqrt{2} + \sqrt{3}$

8. [3 points]

Find the sum of all solutions of

$$4^x - 5 \cdot 2^x + 2 = -8 \cdot 2^{-x}.$$

- ① 1    ② 3    ③ 5    ④ 7    ⑤ 9

9. [3 points]

Simplify  $(3^{\log_{\sqrt{3}} 8}) - \left(\frac{1}{2}\right)^{\log_4 \left(\frac{1}{81}\right)}$ .

- ① 51    ② 53    ③ 55    ④ 57    ⑤ 59

10. [3 points]

When  $2^x = \frac{1}{\sqrt{3}}$  and  $4^y = 27$ , find  $\frac{y}{x}$ .

- ① -1    ② -3    ③ -5    ④ -7    ⑤ -9

11. [3 points]

When  $a = \sqrt{3} + i$  and  $b = \sqrt{3} - i$ , find  $\frac{a^3 - b^3}{ab}$ .

- ①  $2i$     ②  $4i$     ③  $6i$     ④  $8i$     ⑤  $10i$

12. [3 points]

Compute  $\operatorname{tg} \frac{\pi}{8}$ , where  $\operatorname{tg} \theta = \frac{\sin \theta}{\cos \theta}$ .

- ①  $-1 + \sqrt{2}$     ②  $-\frac{1}{2} + \sqrt{2}$     ③  $-\frac{1}{\sqrt{2}} + \sqrt{2}$   
④  $-\frac{1}{3} + \sqrt{2}$     ⑤  $-\frac{1}{\sqrt{3}} + \sqrt{2}$

13. [3 points]

Find the sum of all solutions of

$$3 \cos 2x + 2 \cos x - 1 = 0, \quad (0 \leq x \leq 2\pi).$$

- ①  $\pi$     ②  $\frac{3}{2}\pi$     ③  $2\pi$     ④  $\frac{5}{2}\pi$     ⑤  $3\pi$

14. [3 points]

Find the sum of all solutions of

$$\sqrt{3} \sin x - \cos x = \sqrt{3}, \quad (0 \leq x \leq 2\pi).$$

- ①  $\frac{\pi}{2}$     ②  $\frac{2\pi}{3}$     ③  $\frac{5\pi}{6}$     ④  $\pi$     ⑤  $\frac{4\pi}{3}$

15. [3 points]

When  $A = \begin{pmatrix} 4 & 3 \\ 3 & 2 \end{pmatrix}$ ,  $B = \begin{pmatrix} 1 & 2 \\ -1 & 1 \end{pmatrix}$ , and

$$A^{-1}B^2 = \begin{pmatrix} a & b \\ c & d \end{pmatrix}, \text{ find } a+b+c+d.$$

- ① -6    ② -3    ③ 0    ④ 3    ⑤ 6

16. [3 points]

When  $A = \begin{pmatrix} 1 & 0 \\ 2 & 1 \end{pmatrix}$  and  $A^{100} = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$ ,  
find  $a + b + c + d$ .

- ① 202    ② 204    ③ 206    ④ 208    ⑤ 210

17. [3 points]

Find  $\lim_{x \rightarrow 0} \frac{x^3 + 2 \sin x (1 - \cos x)}{x(1 - \cos x)}$ .

- ① 2    ② 4    ③ 6    ④ 8    ⑤ 10

18. [3 points]

Find  $\lim_{x \rightarrow \infty} (\sqrt{x^3 + 3} - \sqrt{x^3 + 3x\sqrt{x} + 4})$ .

- ①  $-\frac{1}{2}$     ②  $-1$     ③  $-\frac{3}{2}$     ④  $-2$     ⑤  $-\frac{5}{2}$

19. [3 points]

When  $y = ax + b$  is the tangent line to  
 $f(x) = \frac{\sqrt{x+4}}{2x+1}$  at  $x = 0$ , find  $a + b$ .

- ①  $-\frac{1}{4}$     ②  $-\frac{3}{4}$     ③  $-\frac{5}{4}$     ④  $-\frac{7}{4}$     ⑤  $-\frac{9}{4}$

20. [3 points]

Let  $M$  and  $m$  be the maximum and minimum  
values of  $f(x) = \frac{1}{3}x^3 + x^2 - 3x + 1$ ,  
( $-3 \leq x \leq 3$ ), respectively. Find  $M + m$ .

- ①  $\frac{20}{3}$     ②  $\frac{22}{3}$     ③ 8    ④  $\frac{26}{3}$     ⑤  $\frac{28}{3}$

21. [4 points]

Find the minimum value of

$f(x) = 3\sin^2 x - 4\sin x \cos x + 2$ .

- ①  $-2$     ②  $-1$     ③ 0    ④ 1    ⑤ 2

22. [4 points]

When  $\omega = \frac{1 - \sqrt{3}i}{2}$ , find  $\sum_{n=0}^{14} \omega^n$ .

- ① 0    ② 1    ③  $\sqrt{3}i$   
④  $1 - \sqrt{3}i$     ⑤  $\frac{1 - \sqrt{3}i}{2}$

23. [4 points]

When  $f(x) = \sqrt[3]{(3x+2)^4 - 8}$ , find  $f'(0)$ .

- ① 2    ② 4    ③ 6    ④ 8    ⑤ 10

24. [4 points]

When a continuous function  $f: [0, \infty) \rightarrow \mathbb{R}$  satisfies  $\int_0^x f(t^2) dt = x \sqrt{2x^2 + 1}$ , find  $f(4)$ .

- ①  $\frac{11}{3}$     ②  $\frac{13}{3}$     ③  $\frac{14}{3}$     ④  $\frac{16}{3}$     ⑤  $\frac{17}{3}$

25. [4 points]

Find the minimum value of  $f(x) = x^4 + 2x^3 + 4x^2 - 6x + 2$ .

- ①  $\frac{1}{16}$     ②  $\frac{3}{16}$     ③  $\frac{5}{16}$     ④  $\frac{7}{16}$     ⑤  $\frac{9}{16}$

26. [4 points]

Find  $\int_1^4 \frac{x^2 - 2}{\sqrt{x}} dx$ .

- ①  $\frac{42}{5}$     ②  $\frac{44}{5}$     ③  $\frac{46}{5}$     ④  $\frac{48}{5}$     ⑤ 10

27. [4 points]

Find  $\int_0^1 \frac{1}{(2x+1)^3} dx$ .

- ①  $\frac{2}{9}$     ②  $\frac{4}{9}$     ③  $\frac{2}{3}$     ④  $\frac{8}{9}$     ⑤  $\frac{10}{9}$

28. [4 points]

Find  $\lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{k^2 + 2kn - n^2}{n^3}$ .

- ① 1    ②  $\frac{1}{2}$     ③  $\frac{1}{3}$     ④  $\frac{1}{4}$     ⑤  $\frac{1}{5}$

29. [4 points]

When  $\int_0^1 f(2x) dx = 3$  and  $\int_0^3 f(x) dx = 18$ ,

find  $\int_2^3 f(x) dx$ .

- ① 12    ② 14    ③ 16    ④ 18    ⑤ 20

30. [4 points]

Find the area of the region enclosed by  $y = 3x^3 + 2x^2 + x + 5$  and  $y = 3x^3 + x^2 + 4x + 3$ .

- ①  $\frac{1}{2}$     ②  $\frac{1}{3}$     ③  $\frac{1}{4}$     ④  $\frac{1}{5}$     ⑤  $\frac{1}{6}$

## 2023 IUT 1st SBL Answer Sheets

### Type A

No.	1	2	3	4	5	6	7	8	9	10
Ans.	③	④	②	②	③	⑤	①	②	③	②
No.	11	12	13	14	15	16	17	18	19	20
Ans.	②	①	⑤	⑤	⑤	①	②	③	④	⑤
No.	21	22	23	24	25	26	27	28	29	30
Ans.	④	④	④	⑤	③	①	①	③	①	⑤

2023 IUT Admission Test (SOCIE)  
**Math Examination (A TYPE)**

<Multiple choice Types> There is only one correct answer per each question. Mark your answer choice on the OMR answer sheet.

- For each correct answer, you will get the points indicated next to each question number.
- No penalty point is applied to an incorrect answer.

1. [2 points]

Simplify  $\log_2 25 \times \log_3 16 \times \log_{125} 27$ .

- ① 2                      ② 4                      ③ 6  
④ 8                      ⑤ 10

2. [2 points]

Evaluate  $\sum_{n=2}^{10} \frac{1}{n^2 - 1}$ .

- ①  $\frac{6}{11}$       ②  $\frac{3}{5}$       ③  $\frac{36}{55}$       ④  $\frac{39}{55}$       ⑤  $\frac{42}{55}$

3. [2 points]

When  $\alpha, \beta, \gamma$  are solutions of

$x^3 - 4x^2 - 3x + 1 = 0$ , find  $\frac{1}{\alpha} + \frac{1}{\beta} + \frac{1}{\gamma}$ .

- ① 1      ② 2      ③ 3      ④ 4      ⑤ 5

4. [2 points]

When three points  $(1,2), (2,5), (0,a)$  are on a line, find the constant  $a$ .

- ① -2      ② -1      ③ 0      ④ 1      ⑤ 2

5. [2 points]

When  $\omega = \frac{-1 + \sqrt{3}i}{2}$ , evaluate  $\sum_{n=1}^{20} \omega^n$ .

- ① -1                      ② -i                      ③ 0  
④ 1                      ⑤ i

6. [2 points]

When  $e^{2x} = 5$ , find  $\frac{e^{3x} - e^{-3x}}{e^x - e^{-x}}$ .

- ①  $\frac{23}{5}$       ② 5      ③  $\frac{27}{5}$       ④  $\frac{29}{5}$       ⑤  $\frac{31}{5}$

7. [3 points]

When  $3 \cos 2\theta + 3 = 16 \sin \theta$ , find  $\sin \theta$ .

- ①  $\frac{1}{6}$       ②  $\frac{1}{3}$       ③  $\frac{1}{2}$       ④  $\frac{2}{3}$       ⑤  $\frac{5}{6}$

8. [3 points]

Find the sum of all integer solutions of

$$x^4 - 5x^3 - x^2 + 5x < 0.$$

- ① 1    ② 3    ③ 5    ④ 7    ⑤ 9

9. [3 points]

When a sequence  $\{a_n\}_{n=1}^{\infty}$  satisfies

$$\sum_{k=1}^n ka_k = n^2 + 3n,$$

find  $a_{10}$

- ① 2    ②  $\frac{11}{5}$     ③  $\frac{12}{5}$     ④  $\frac{13}{5}$     ⑤  $\frac{14}{5}$

10. [3 points]

When  $A = \begin{pmatrix} 1 & 2 \\ -1 & 2 \end{pmatrix}$ ,  $B = \begin{pmatrix} 2 & 4 \\ 4 & 2 \end{pmatrix}$ , find the sum of all entries of  $A^{-1}B$ .

- ① -3    ②  $-\frac{3}{2}$     ③ 0  
④  $\frac{3}{2}$     ⑤ 3

11. [3 points]

When  $\alpha, \beta$  are solutions of  $(e^x - 2)(e^x - 4) = 1$ , find  $\alpha + \beta$ .

- ① 0    ②  $\ln 3$     ③  $\ln 5$     ④  $\ln 7$     ⑤  $\ln 9$

12. [3 points]

Compute  $\lim_{x \rightarrow 0} \frac{e^x + e^{-x} - 2}{x^2}$ .

- ① 1    ②  $\frac{3}{2}$     ③ 2    ④  $\frac{5}{2}$     ⑤ 3

13. [4 points]

When  $f(x) = x^3 + 3x^2 - 6x + 1$  and  $g(x) = f(\sin \pi x + x)$ , find  $g'(1)$ .

- ①  $-3\pi - 3$     ②  $-3\pi + 3$     ③ 0  
④  $3\pi - 3$     ⑤  $3\pi + 3$

14. [4 points]

When  $\theta$  is the angle between the  $z$ -axis and the plane  $x + 2y + 3z = 2$ , find  $\cos \theta$ .

- ①  $\frac{\sqrt{50}}{14}$     ②  $\frac{\sqrt{15}}{7}$     ③  $\frac{\sqrt{70}}{14}$   
④  $\frac{\sqrt{20}}{7}$     ⑤  $\frac{\sqrt{90}}{14}$

15. [4 points]

Evaluate  $\int_0^1 \frac{x}{(x^2 + 1)^2} dx$ .

- ①  $\frac{1}{8}$     ②  $\frac{1}{4}$     ③  $\frac{3}{8}$     ④  $\frac{1}{2}$     ⑤  $\frac{5}{8}$

16. [4 points]

Evaluate  $\int_0^\pi x \sin x \, dx$ .

- ①  $\pi$       ②  $\frac{3}{2}\pi$       ③  $2\pi$       ④  $\frac{5}{2}\pi$       ⑤  $3\pi$

17. [4 points]

When  $\int_0^1 f(x) \, dx = 2$  and  $\int_0^3 f(x) \, dx = 5$ ,

find  $\lim_{n \rightarrow \infty} \frac{1}{n} \sum_{k=1}^n f\left(1 + \frac{2k}{n}\right)$ .

- ①  $\frac{3}{2}$       ②  $2$       ③  $\frac{5}{2}$       ④  $3$       ⑤  $\frac{7}{2}$

18. [5 points]

Find the distance between the line  $y = x + 2$  and the curve  $y = x - x^2$ .

- ①  $\frac{\sqrt{2}}{4}$       ②  $\frac{\sqrt{2}}{2}$       ③  $\frac{3\sqrt{2}}{4}$   
④  $\sqrt{2}$       ⑤  $\frac{5\sqrt{2}}{4}$

19. [5 points]

Find the area of the triangle with three vertices  $(1, 2, 3)$ ,  $(1, 1, 1)$ ,  $(2, 2, 1)$ .

- ①  $\frac{1}{2}$       ②  $1$       ③  $\frac{3}{2}$   
④  $2$       ⑤  $\frac{5}{2}$

20. [5 points]

Find the area between two curves:

$$y = x^3 + 2x, \quad y = x^2 + 3x - 1.$$

- ①  $\frac{1}{3}$       ②  $\frac{2}{3}$       ③  $1$   
④  $\frac{4}{3}$       ⑤  $\frac{5}{3}$

21. [5 points]

When  $f(x) = e^x + x$  and  $g$  is the inverse function of  $f$ , find  $\int_1^{e+1} g(x) \, dx$ .

- ①  $\frac{1}{2}$       ②  $\frac{3}{4}$       ③  $1$   
④  $\frac{5}{4}$       ⑤  $\frac{3}{2}$



# 2023 IUT Admission Test(SOCIE) Answers & solutions

## -Type A

1	2	3	4	5	6	7
④	③	③	②	①	⑤	②
8	9	10	11	12	13	14
⑤	②	⑤	④	①	②	③
15	16	17	18	19	20	21
②	①	①	④	③	④	⑤

## -Type B

1	2	3	4	5	6	7
③	④	③	⑤	②	①	②
8	9	10	11	12	13	14
②	⑤	①	⑤	④	②	②
15	16	17	18	19	20	21
③	①	①	④	④	③	⑤

## -Type C

1	2	3	4	5	6	7
①	⑤	④	③	③	②	④
8	9	10	11	12	13	14
①	②	⑤	②	⑤	①	①
15	16	17	18	19	20	21
②	③	②	④	⑤	④	③

## -Type D

1	2	3	4	5	6	7
③	④	②	③	⑤	①	⑤
8	9	10	11	12	13	14
②	⑤	②	①	④	③	②
15	16	17	18	19	20	21
①	②	①	③	④	⑤	④

## Solutions of SOCIE, type A

1.  $\log_2 25 \times \log_3 16 \times \log_{125} 27 = \frac{2\log 5}{\log 2} \times \frac{4\log 2}{\log 3} \times \frac{3\log 3}{3\log 5} = 8.$

2.  $\sum_{n=2}^{10} \frac{1}{n^2-1} = \frac{1}{2} \sum_{n=2}^{10} \left( \frac{1}{n-1} - \frac{1}{n+1} \right) = \frac{1}{2} \left( 1 + \frac{1}{2} - \frac{1}{10} - \frac{1}{11} \right) = \frac{36}{55}.$

3.  $\frac{1}{\alpha} + \frac{1}{\beta} + \frac{1}{\gamma} = \frac{\alpha\beta + \beta\gamma + \gamma\alpha}{\alpha\beta\gamma} = 3.$

4. Since  $\frac{5-2}{2-1} = \frac{a-2}{0-1}$ , we have  $a = -1.$

5. Since  $1 + \omega + \omega^2 = 0$ , we have  $\sum_{n=1}^{20} \omega^n = \omega + \omega^2 = -1.$

6.  $\frac{e^{3x} - e^{-3x}}{e^x - e^{-x}} = \frac{e^{6x} - 1}{e^{2x}(e^{2x} - 1)} = \frac{5^3 - 1}{5 \times 4} = \frac{31}{5}.$

7. Since  $3(1 - 2\sin^2\theta) + 3 = 16\sin\theta$ , we get  $(3\sin\theta - 1)(\sin\theta + 3) = 0$ , hence  $\sin\theta = \frac{1}{3}.$

8. Since  $x^4 - 5x^3 - x^2 + 5x = x(x-1)(x+1)(x-5) < 0$ , we get  $-1 < x < 0$ ,  $1 < x < 5$ , hence the sum of integer solutions is 9.

9. Since  $10a_{10} = 10^2 + 3 \times 10 - (9^2 + 3 \times 9) = 22$ , we have  $a_{10} = \frac{11}{5}.$

10.  $A^{-1}B = \frac{1}{4} \begin{pmatrix} 2 & -2 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} 2 & 4 \\ 4 & 2 \end{pmatrix} = \begin{pmatrix} -1 & 1 \\ 3 & 3 \\ 2 & 2 \end{pmatrix}.$

Therefore the sum of all the elements of  $A^{-1}B$  is 3.

11. Since  $(e^x - 2)(e^x - 4) - 1 = (e^x - e^\alpha)(e^x - e^\beta)$ , we get  $e^{\alpha+\beta} = 7$  so that  $\alpha + \beta = \ln 7.$

12. By L'hospital theorem, we get  $\lim_{x \rightarrow 0} \frac{e^x + e^{-x} - 2}{x^2} = \lim_{x \rightarrow 0} \frac{e^x - e^{-x}}{2x} = \lim_{x \rightarrow 0} \frac{e^x + e^{-x}}{2} = 1.$

13. Since  $g'(x) = f'(\sin\pi x + x) \times (\pi\cos\pi x + 1)$ , we get  $g'(1) = f'(1) \times (-\pi + 1) = -3\pi + 3.$

14. Since  $\sin\theta = \frac{(1,2,3) \cdot (0,0,1)}{|(1,2,3)| \times |(0,0,1)|} = \frac{3}{\sqrt{14}}$ , we get  $\cos\theta = \sqrt{1 - \left(\frac{3}{\sqrt{14}}\right)^2} = \frac{\sqrt{70}}{14}.$

$$15. \int_0^1 \frac{x}{(x^2+1)^2} dx = \left[ -\frac{1}{2(x^2+1)} \right]_0^1 = \frac{1}{4}.$$

16. By integration by parts, we get

$$\int_0^\pi x \sin x dx = -x \cos x \Big|_0^\pi + \int_0^\pi \cos x dx = \pi.$$

$$17. \lim_{n \rightarrow \infty} \frac{1}{n} \sum_{k=1}^n f\left(1 + \frac{2k}{n}\right) = \frac{1}{2} \int_1^3 f(x) dx = \frac{5-2}{2} = \frac{3}{2}.$$

18. Since  $y=x$  is tangent to  $y=x-x^2$ , the distance between  $y=x-x^2$  and  $y=x+2$  is equal to the distance between  $y=x$  and  $y=x+2$ . Therefore the distance is  $\sqrt{2}$ .

19. Let  $a = (1, 2, 3) - (1, 1, 1) = (0, 1, 2)$ ,  $b = (2, 2, 1) - (1, 1, 1) = (1, 1, 0)$ . Then the area of the triangle is

$$\frac{1}{2} \sqrt{|a|^2|b|^2 - (a \cdot b)^2} = \frac{1}{2} \sqrt{5 \times 2 - 1} = \frac{3}{2}.$$

20. Since  $x^3 + 2x - (x^2 + 3x - 1) = (x+1)(x-1)^2$ , the area between two curves  $y = x^3 + 2x$ ,  $y = x^2 + 3x - 1$  is

$$\int_{-1}^1 (x+1)(x-1)^2 dx = 2 \int_0^1 (-x^2 + 1) dx = \frac{4}{3}.$$

21. Let  $t = g(x)$ . Then  $\int_1^{e+1} g(x) dx = \int_0^1 t f'(t) dt = t f(t) \Big|_0^1 - \int_0^1 f(t) dt = e + 1 - (e - \frac{1}{2}) = \frac{3}{2}$ .

2023 IUT Admission Test(SOCIE)

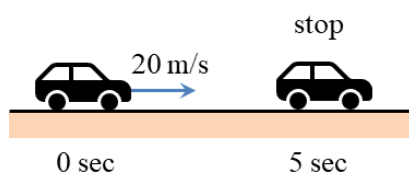
# Physics Examination(A TYPE)

<Multiple choice Types> There is only one correct answer per each question. Mark your answer choice on the OMR answer sheet.

- For each correct answer, you will get the points indicated next to each question number.
- No penalty point is applied to an incorrect answer.

1. [3 points]

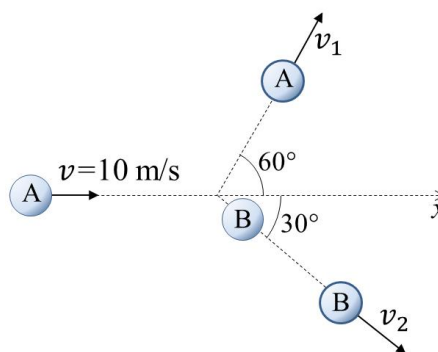
As shown in the figure below, a car running at a speed of 20 m/s in the east direction stopped after 5 seconds. What is the average acceleration during 5 seconds?



- ① 4 m/s<sup>2</sup> to the west      ② 2 m/s<sup>2</sup> to the west
- ③ 4 m/s<sup>2</sup> to the east      ④ 2 m/s<sup>2</sup> to the east
- ⑤ 2 m/s<sup>2</sup> to the south

2. [5 points]

As shown in the figure below, a ball A moving at a speed of  $v = 10$  m/s in the  $x$ -direction on a horizontal plane collides elastically with a ball B of the same mass that is at rest. After the collision, the speeds of A and B are  $v_1$  and  $v_2$ , respectively, and the directions of motion of A and B form an angle of  $60^\circ$  and  $30^\circ$  with the  $x$ -axis, respectively. Find the speeds  $v_1$  and  $v_2$  after the collision.



- ①  $5\sqrt{3}$  m/s, 5 m/s      ② 6 m/s, 8 m/s
- ③ 5 m/s,  $5\sqrt{3}$  m/s      ④ 8 m/s, 6 m/s
- ⑤  $2\sqrt{5}$  m/s,  $4\sqrt{5}$  m/s

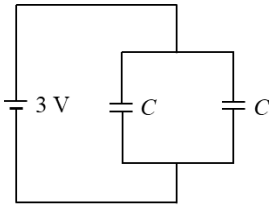
3. [3 points]

A certain amount of ideal gas changes from state A (volume  $2 \times 10^{-3}$  m<sup>3</sup>, pressure  $5 \times 10^5$  Pa, temperature 300 K) to state B (volume  $1 \times 10^{-3}$  m<sup>3</sup>, pressure  $2 \times 10^5$  Pa). What is the temperature of state B?

- ① 50 K      ② 60 K      ③ 80 K
- ④ 100 K      ⑤ 120 K

4. [3 points]

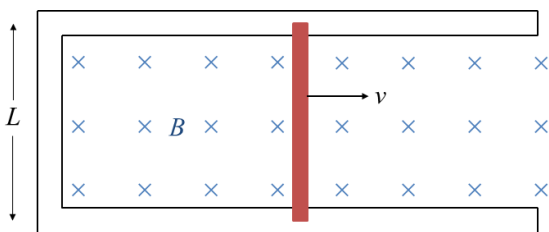
As shown in the figure below, two capacitors with capacitance  $C$  of  $1.5 \times 10^{-6} \text{ F}$  are connected in parallel and connected to a 3 V power supply. What is the total charge stored in the capacitors?



- ①  $3 \mu\text{C}$     ②  $5 \mu\text{C}$     ③  $6 \mu\text{C}$   
 ④  $8 \mu\text{C}$     ⑤  $9 \mu\text{C}$

5. [4 points]

As shown in the figure below, a C-shaped conducting rail is placed vertically in a uniform magnetic field of  $B = 0.40 \text{ T}$  and a rod with a length of  $L = 0.30 \text{ m}$  is placed on top of it. The rod is forced to move at constant speed  $v = 5.0 \text{ m/s}$  along horizontal rails. The rod and rails form a conducting loop. The rod has resistance  $0.40 \Omega$ ; the rest of the loop has negligible resistance. What is the magnitude of the force that must be applied to the rod to make it move at constant speed?



- ①  $0.12 \text{ N}$     ②  $0.15 \text{ N}$     ③  $0.16 \text{ N}$   
 ④  $0.18 \text{ N}$     ⑤  $0.20 \text{ N}$

6. [3 points]

There is a wave that oscillates 4 times per second. What is the speed of propagation of this wave if it travels 20 cm during one oscillation?

- ①  $0.5 \text{ m/s}$     ②  $0.6 \text{ m/s}$     ③  $0.8 \text{ m/s}$   
 ④  $1.0 \text{ m/s}$     ⑤  $1.2 \text{ m/s}$

7. [3 points]

When an object is placed 10 cm in front of a convex mirror, a virtual image 0.5 times the size of the object is created. What is the focal length of this convex mirror?

- ①  $10 \text{ cm}$     ②  $12 \text{ cm}$     ③  $15 \text{ cm}$   
 ④  $20 \text{ cm}$     ⑤  $25 \text{ cm}$

8. [3 points]

The temperature of the surface of the blackbody is doubled from  $T$  to  $2T$ . How many times will be the intensity of the energy ( $I$ ) emitted from the black body and the wavelength ( $\lambda_{\text{max}}$ ) at which the intensity of the emitted energy is maximized, respectively?

- ① 16 times,  $\frac{1}{4}$  times    ② 16 times,  $\frac{1}{2}$  times  
 ③ 8 times,  $\frac{1}{4}$  times    ④ 8 times,  $\frac{1}{2}$  times  
 ⑤ 4 times,  $\frac{1}{4}$  times

9. [3 points]

Choose the correct pairing of phenomena that only waves can exhibit.

- ① reflection, refraction    ② reflection, interference  
 ③ refraction, interference    ④ refraction, diffraction  
 ⑤ interference, diffraction

# Physics Examination(A TYPE) Answers

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<Multiple choice Types> There is only one correct answer per each question. Mark your answer choice on the OMR answer sheet.

- For each correct answer, you will get the points indicated next to each question number.
- No penalty point is applied to an incorrect answer.

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Answers:

1. ①
2. ③
3. ②
4. ⑤
5. ④
6. ③
7. ①
8. ②
9. ⑤